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A COMPILATION OF CURRENT COMPUTER PROGRAMS FOR LOW-THRUST TRAJECTORY ANALYSIS

by Alfred C. Mascy

NASA Headquarters

Mission Analysis Division

Moffett Field, Calif.

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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TABLE OF CONTENTS

	<u>Page</u>
SUMMARY	1
INTRODUCTION	1
SYMBOLS	2
COMPILATION OF PROGRAM DESCRIPTIONS	2
INDEX OF PROGRAMS	3

A COMPILATION OF CURRENT COMPUTER PROGRAMS

FOR LOW-THRUST TRAJECTORY ANALYSIS

By Alfred C. Masey

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SUMMARY

This paper provides a catalogue of brief descriptions of current low-thrust trajectory and mass computation programs. All known sources were contacted, and questionnaires were sent to those who indicated that they possessed such codes. A total of 59 descriptions of computer programs pertinent to this discipline are compiled. They are capable of generating flyby and rendezvous trajectories with their associated mass computation. Included in the codes are those capable of variable thrust trajectory as well as constant thrust with coast trajectory calculations. No attempt is made to evaluate any computer code or in any way compare programs; rather, the descriptions of existing codes are presented. Further details concerning a particular program may be obtained from the organization shown on each description. Many programs are well documented, and all organizations are encouraged to use the services provided by the regional dissemination center, COSMIC, located at the University of Georgia and sponsored by the NASA Office of Technology Utilization.

INTRODUCTION

There is increasing interest in the application of advanced propulsion systems, such as electric rockets, to advanced missions having high velocity requirements. Better utilization of existing computer programs, or the development of new codes supplemented by experience with existing programs, is needed to define these requirements. This survey indicates that numerous low-thrust computer programs now exist, but many are not reported in the literature. The majority of these programs are worthwhile and can be of greater use if they are made known to the community of low-thrust analysts.

Thus, the purpose of this paper is to provide a catalogue of brief descriptions of current low-thrust trajectory computer programs. This paper does not attempt to evaluate any computer code or to compare one program with another. The descriptions of computer codes pertinent to low-thrust mission analysis serve only to introduce the respective programs in order to advance research in this area by the exchange of ideas, trajectory concepts, and mathematical methods already applied.

Gratitude is expressed to all organizations participating in this survey; they gave freely of their time and information to enhance the scope of this work.

SYMBOLS

a_0	initial acceleration
I_{sp}	specific impulse of thruster
$\frac{T}{W}$	thrust-to-weight ratio
V_∞	hyperbolic excess speed
α	power-plant specific mass
η	efficiency of thrusters
μ_L	payload mass fraction
μ_p	propellant mass fraction
μ_w	power-plant mass fraction

COMPILATION OF PROGRAM DESCRIPTIONS

All organizations that might possess a low-thrust computer program capability were contacted. After an initial contact by telephone, questionnaires (see sample on page 7) were sent to the individuals who wished to participate in the survey. The data on each completed questionnaire were transferred to an information sheet that did not include the multiple choice or nonapplicable answers. Some questionnaires were only partially completed but were accompanied by the program documentation, which was transferred to the information sheet. It is hoped that this transfer was done as accurately as the programmer would have done it. Copies of the information were sent to all participants for their comments, corrections, and updating. The present publication reflects all changes.

A total of 59 descriptions of programs pertinent to low-thrust trajectory and mass computation are compiled (pp. 8-66). It is believed that these represent most of the codes in this discipline. These descriptions represent approximately 52 different programs; many have been modified and are described as slightly different codes by various users. Rather than screen a program that may have been modified for the user's needs, all low-thrust code descriptions submitted have been included in this compilation. However, some programs were not directly applicable to low-thrust trajectory analysis and have not been included in this survey.

There are about twice as many two-dimensional codes as there are three-dimensional codes. Most two-dimensional codes utilize a polar coordinate system, while most three-dimensional programs use a Cartesian system. Only two programs actually appear to account for more than the usual two bodies in

a gravitational system. Most codes have been programmed in Fortran IV, although a few require a knowledge of machine language. Most codes do require initial guesses such as the Lagrange multipliers; however, a few programs generate the necessary starting values from an approximate solution, such as a circular arc trajectory or an iterated circle start solution. A few programs are applicable only to the planetocentric phase, and the others are flyby and rendezvous decks; most programs are capable of both operations. There is an almost total absence of round-trip trajectory codes. Approximately 15 percent of the codes include some estimate of the planetocentric phase, as well as the heliocentric phase.

Potential users who are interested in further information on the programs are advised to contact the respective company. Many programs are well documented, and all organizations are encouraged to submit them to COSMIC for inclusion in the library of available programs. COSMIC is one of the newest regional dissemination centers located at the University of Georgia and sponsored by the NASA Office of Technology Utilization. In general, its purpose is to acquire and disseminate information and software (card decks, tapes, etc.) on technical and scientific computer programs originated during NASA work. Once a program is accepted by COSMIC, the authoring organization no longer needs to prepare and transmit its program to potential users. Organizations are encouraged to use the dissemination service.

INDEX OF PROGRAMS

<u>Page</u>	<u>Company/Organization</u>	<u>Name of Program</u>
7	Sample Questionnaire	
8	Aerofet General, Space General Plant	ORPERT
9	AFIT-SEE, Wright-Patterson AFB	Low-Thrust Solar Probe
10	Analytical Mechanics Associ- ates	2-Body Trajectory Optimization Program
11	Analytical Mechanics Associ- ates	Second Variation Rocket Trajec- tory Optimization Program
12	AVCO	#1546 - Generalized Variation of Parameters Program
13	Bell Telephone Laboratories	DEPAK; MULTI
14	Boeing/Space Division	Variable Thrust Polynomial Optimizer
15	Boeing/Space Division	Space Trajectory Optimization Program (AS 2080)
16	Colorado State University	Characteristic Length Method
17	Computer Applications, Inc.	
18	Connecticut University, Aero- space Engineering Dept.	PDER, PDERDP (double precision version)
19	General Dynamics/Convair	Convair Low-Thrust Optimization Programs
20	General Dynamics/Fort Worth	Y28 Optimum Low-Thrust Procedure
21	General Dynamics/Fort Worth	Low-Thrust Trajectory Optimization
22	General Dynamics/Fort Worth	Interplanetary Low-Acceleration Constant-Thrust Trajectory Patching Program
23	General Dynamics Fort/Worth	Low-Thrust Propulsion System Optimization Program
24	General Electric Company	POLAR
25	General Electric - M&SD	Finite Burn Orbit Insertion Program
26	Goddard Space Flight Center, NASA	Variable Power, Variable Thrust Option/F369
27	Goddard Space Flight Center, NASA	Low-Thrust Trajectory Subprogram
28	Grumman Aircraft	Low-Thrust Interplanetary Trajectory Optimization

<u>Page</u>	<u>Company/Organization</u>	<u>Name of Program</u>
29	Hayes International Corp.	Orbital Elements for Low-Thrust Trajectories
30	Hayes International Corp.	Quasi-Steady Orbital Rendezvous
31	Hughes Aircraft Company	Low-Thrust Trajectory
32	IBM Federal Systems Division	OPGUIDE
33	IIT Research Institute	LTNAV-1 (Low-Thrust Navigation Analysis)
34	IIT Research Institute	LTNAV-2 (Low-Thrust Planetocentric Navigation Analysis)
35	JPL	Optimum Thrust Programs for Power Limited Propulsion Systems (1016000)
36	JPL	ASTRAL
37	JPL	MALTS
38	Langley Research NASA	PRESTO (DELTA)
39	Langley Research Center, NASA	TOMSD (Trajectory Optimization by Method of Steepest Descent)
40	Lewis Research Center, NASA	Lewis N-Body Code
41	Lewis Research Center, NASA	MAXIM
42	Lockheed Missiles and Space Company, Research Labora- tories	Low-Thrust Heliocentric Transfers
43	Lockheed Missiles & Space Company, Research Labora- tories	Low-Thrust Escape From Planet
44	Lockheed Missiles & Space Company	LTCOMP
45	Los Alamos Scientific Laboratory	1965 Version, Produced by Dept. of Aerospace and Mechanical Sciences, Princeton University, Report No. 7170-1
46	McDonnell Douglas Astronautics	FYNDIF
47	McDonnell Douglas Astronautics	LOW TOP
48	McDonnell Douglas Astronautics	WHAMO
49	McDonnell Douglas Astronautics	HITOP

<u>Page</u>	<u>Company/Organization</u>	<u>Name of Program</u>
50	North American Rockwell Corp., Space Division	Optimum Trajectory Program for Power-Limited Propulsion Systems
51	OART, Mission Analysis Division, NASA	BABE
52	OART, Mission Analysis Division, NASA	QUICKLY
53	Princeton University, ASMAR	Lion 1
54	Princeton University, ASMAR	Campbell 1 (modified item)
55	Princeton University, ASMAR	Gordon 2
56	Princeton University, ASMAR	PRIMER
57	Rand Corporation	ROCKET
58	RCA/Astro Electronics Division	Gordon 2
59	System Sciences Corp. (subsidiary of Computer Science Corp.)	High-Precision, Low-Thrust Integration and Optimization Program
60	Texas University	NMS
61	TRW Systems	MALTS, Mission Analysis & Simulation Program
62	United Aircraft Research Laboratories	Mass Ratio Optimization (simplified and improved payload fraction definition) F487
63	United Aircraft Research Laboratories	High and Low Thrust Mass Optimization/F211
64	United Aircraft Research Laboratories	Mass Ratio Optimization (simplified payload fraction) F530
65	United Aircraft Research Laboratories	Variable Power, Variable Thrust Option/F369
66	United Aircraft Research Laboratories	Constant-Thrust, Multiple-Coast/F615

LOW-THRUST TRAJECTORY AND MASS COMPUTATION PROGRAM

Company Organization :
Name of Program :
Authors/Contact :
Program Funded by : i.e., company, NASA contract, . . .

Description

(Please circle or add appropriate comment.)

Number of Dimensions : i.e., 1, 2, 3
Number of Bodies : i.e., 2, 3, . . .
Coordinate System : i.e., Cartesian, polar, . . .
Integration Technique : i.e., variable step, fixed step, . . .
Program Language : i.e., Fortran IV, II, . . .
Computer Now Used : i.e., IBM 7094, CDC 6600, Univac 1108, . . .
Trajectory Options : i.e., flyby, rendezvous, round trip, . . .
Specific Impulse : i.e., variable, constant, . . .
Power Options : i.e., constant, function of time, function of
distance, . . .
Other Options : . . .
Input (briefly) : i.e., position and velocity, Julian dates, hyper-
bolic excess velocity, ISP, powerplant specific
mass, α , . . .
Initial Guesses Required: i.e., Lagrange multipliers, T/W, . . .
Parameters Optimized : i.e., ISP, T/W₀, μ_w , V_∞ , power level, $\int a^2 dt$,
coast time, thrust angle, . . .
Optimization Technique : i.e., gradient method, Newton-Raphson, . . .
Output (briefly) : i.e., time history, ISP, T/W, payload, $\int a^2 dt$, . . .
Planetocentric Phase : not included in program, high-thrust capture and
departure, low-thrust spiralling, . . .
Limitations of Program : i.e., travel angle, T/local g, . . .
Other Applications of Program _____
Documentation of Program _____
Availability to Other Users _____
Other Comments _____

Please Mail Completed Form to: Alfred C. Masey
NASA Mission Analysis Division, OART
Mail Stop 202-8
Moffett field, California 94035

Company/Organization : Aerojet General, Space General Plant,
El Monte, California

Name of Program : ORPERT

Authors/Contact : Dr. Leonard Pode/Wayne F. Brady

Program Funded by : Company

Description

Number of Dimensions : 3

Number of Bodies : Up to 5 satellites and Earth, Sun and Moon
currently

Coordinate System : Cartesian

Integration Technique : Fixed step

Program Language : Fortran IV

Computer Now Used : IBM 360/40

Trajectory Options : Currently written for Earth orbit

Specific Impulse : Constant

Input (briefly) : Position and velocity, Julian dates, time to
start & stop thrust, direction of thrust WRT
VEL vector, magnitude of thrust, weight flow
rate

Output (briefly) : Time history

Limitations of Program : Eccentricity $\neq 0$

Other Applications : Will handle up to 5 satellites in Earth orbit;
includes perturbations due to atmosphere,
Earth harmonics, Moon & Sun

Documentation : A report is in rough draft.

Availability : Program not completed due to funding.

Other Comments : JPL ephemeris tape used. Conversion to another
gravitational center would not be difficult.
Program originally written to simulate
deployment and separation history of several
satellites in orbit.

Company/Organization : AFIT-SEE, W-Patterson AFB, Ohio 45433
 Name of Program : Low-Thrust Solar Probe
 Authors/Contact : Major Roger W. Johnson/Capt. H. T. Brock

Description

Number of Dimensions : 2
 Number of Bodies : 2
 Coordinate System : Polar
 Integration Technique : Variable step
 Program Language : Fortran IV
 Computer Now Used : IBM 7094
 Trajectory Options : Flyby
 Power Options : Constant
 Input (briefly) : Position and velocity
 Initial Guesses Required : T/W
 Parameters Optimized : $\int a^2 dt$
 Optimization Technique : Newton-Raphson
 Output (briefly) : Time history
 Planetocentric Phase : Not included in program
 Limitations of Program : Travel angle
 Other Applications : Available approximately June 1968
 Documentation : Thesis form
 Availability : Yes (listing)

Company/Organization	: Analytical Mechanics Associates, Inc.
Name of Program	: 2-Body Trajectory Optimization Program
Authors/Contact	: J. H. Campbell
Program Funded by	: Sub-contract from Princeton

Description

Number of Dimensions	: 3
Number of Bodies	: N
Coordinate System	: Cartesian
Integration Technique	: In mass ratio
Program Language	: Fortran IV
Computer Now Used	: IBM 360
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Constant, function of distance
Input (briefly)	: Position and velocity, Julian dates, hyperbolic excess velocity, ISP, powerplant specific mass, alpha, launch vehicle, sizing parameters, etc.
Initial Guesses Required	: Lagrange multipliers, T/W, and any unspecified initial conditions
Parameters Optimized	: ISP, T/W_0 , V_∞ , coast time, thrust angle, t_0 , t_f
Optimization Technique	: Employs indirect method coupled with gradient method for solution of boundary value problem
Planetocentric Phase	: High-thrust departure
Documentation	: In progress
Availability	: Available at Princeton U. and GSFC

Company/Organization	: Analytical Mechanics Associates, Inc.
Name of Program	: Second Variation Rocket Trajectory Optimization Program
Authors/Contact	: Dr. Henry J. Kelley, Westbury, N. Y. Office
Program Funded by	: Various NASA MSC contracts

Description

Number of Dimensions	:	3
Number of Bodies	:	2
Coordinate System	:	Cartesian
Integration Technique	:	Fixed step Runge-Kutta
Program Language	:	Fortran IV
Computer Now Used	:	IBM 360
Trajectory Options	:	Rendezvous and orbit transfer options
Specific Impulse	:	Constant
Power Options	:	Constant or solar
Input (briefly)	:	Initial and terminal conditions
Initial Guesses Required	:	First guess on steering history
Parameters Optimized	:	Steering histories and switch times
Optimization Technique	:	Second variation
Output (briefly)	:	Time history of control, state and multipliers
Planetocentric Phase	:	Not included
Limitations of Program	:	Program is primarily high-thrust, but should handle low-thrust heliocentric well.
Documentation	:	Presently undocumented
Availability	:	Has been used exclusively in-house
Reference	:	"A Trajectory Optimization Technique Based Upon the Theory of the Second Variation," H. J. Kelly, R. E. Kopp and H. G. Moyer, AIAA No. 63-415, Aug. 19, 1963.

Company/Organization	: Bell Telephone Laboratories
Name of Program	: DEPAK; MULTI
Authors/Contact	: A. J. Claus
Program Funded by	: Company

Description

Number of Dimensions	: 3
Number of Bodies	: 3
Coordinate System	: Cartesian
Integration Technique	: Variable step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094, GE 635
Specific Impulse	: Variable, constant
Power Options	: Constant, function of time, function of distance
Input (briefly)	: Position and velocity, Julian dates, ISP
Output (briefly)	: Time history
Documentation	: Internal memoranda
Availability	: Written request addressed to Bell Labs required
Other Comments	: The program is essentially a general purpose numerical integration package with variable stepsize and operating in either single (8 digits) or double (16 digits) precision.

Company/Organization : The Boeing Co./Space Division - Guidance and Control

Name of Program : Variable Thrust Polynomial Optimizer

Authors/Contact : Forrester Johnson/Daril Hahn

Program Funded by : Company

Description

Number of Dimensions : 3

Number of Bodies : 2

Coordinate System : Cartesian

Integration Technique : Does not integrate

Program Language : Fortran IV

Computer Now Used : Univac 1108

Trajectory Options : Flyby, rendezvous

Specific Impulse : Variable

Power Options : Constant

Input (briefly) : Position and velocity, Julian dates, hyperbolic excess velocity, Isp

Initial Guesses Required : Self generating

Parameters Optimized : $\int a^2 dt$

Optimization Technique : Newton-Raphson

Output (briefly) : Time history, $a^2 dt$

Planetocentric Phase : Not included in program

Availability : Decided on an individual basis

Other Comments : Uses an approximate, but rapid, method

Company/Organization : The Boeing Company/Space Div., Guidance and Control Organization

Name of Program : Space Trajectory Optimization Program (AS 2080)

Authors/Contact : D. W. Hahn, Berdein F. Itzen

Program Funded by : Company

Description

Number of Dimensions : 3

Number of Bodies : 2

Coordinate System : Polar

Integration Technique : Fixed step

Program Language : Fortran IV

Computer Now Used : Univac 1108

Trajectory Options : Flyby, rendezvous

Specific Impulse : Constant

Power Options : Constant, function of distance

Other Options : Planetocentric high-thrust departure to an input c_3

Input (briefly) : Position and velocity, Isp, V_∞

Initial Guesses Required : Control schedule

Parameters Optimized : Coast times, thrust angle, final mass

Optimization Technique : Gradient method

Output (briefly) : Time history, payload

Planetocentric Phase : High-thrust capture and departure; low-thrust spiralling

Other Applications : General orbit transfer maneuvers, any thrust level

Documentation : Documented except for recent revisions

Availability : Considered on an individual basis

Company/Organization	: Colorado State University
Name of Program	: Characteristic Length Method
Authors/Contact	: Professor W. R. Mickelsen, Dept. of Mech. Eng.
Program Funded by	: NASA Grant NGR06-002-032
	<u>Description</u>
Integration Technique	: Program does not compute trajectory.
Program Language	: Fortran IV
Computer Now Used	: CDC 6400
Trajectory Options	: Flyby, rendezvous, round trip, etc.
Specific Impulse	: Variable, constant, other
Power Options	: Constant, function of time, function of distance
Input (briefly)	: Hyperbolic excess speed and transfer time from impulsive thrust trajectories, launch vehicle payload versus V_{∞} , α of total electric propulsion system, I_{sp} , T/W_0
Initial Guesses Required	: Propulsion time
Parameters Optimized	: I_{sp} , T/W_0 , V_{∞} (by inspection of output)
Output (briefly)	: <u>Approximate</u> values of propulsion time, final mass of electric stage, final payload
Planetocentric Phase	: High-thrust capture and departure
Limitations of Program	: Trajectory similarity
Documentation	: AIAA Paper No. 67-709
Availability	: Upon request
Other Comments	: The characteristic-length method is based on a nonrigorous assumption of similarity between low-thrust and impulsive-thrust trajectories. Although the output is only approximate, it may serve well as a fast source for first guess inputs to complex programs.
Reference	: Zola, Charles L.: A Method of Approximating Propellant Requirements of Low-Thrust Trajectories. NASA TN D-3400, 1966.

Company/Organization : Computer Applications, Inc.

Authors/Contact : Moshe Mangad, Ph.D.

Description

Number of Dimensions : 2, 3

Number of Bodies : 2, 3, 4

Coordinate System : Cartesian, polar, nondimensional (i.e., Perkins Units)

Integration Technique : Variable and constant

Program Language : Fortran IV

Computer Now Used : IBM 7090/94, 704, Philco 5200

Trajectory Options : Flyby, rendezvous, moon transfer

Specific Impulse : Constant and variable

Power Options : Constant, function of time, distance

Other Options : Coast period as $f(t, d)$, $\dot{f}(t)$, or $f(d)$

Input (briefly) : Position and velocity, vehicle/payload constraints

Initial Guesses Required : T/W

Parameters Optimized : Isp, V_∞ , power level, T/W₀

Optimization Technique : Gradient method

Output (briefly) : Time history, Isp, T/W

Planetocentric Phase : Low thrust spiralling

Other Applications : Logistics study of Moon transfer

Other comments : 4-body problem done for hyperbolic encounter study.

Company/Organization	: University of Connecticut, Aerospace Engineering Dept.
Name of Program	: PDER, PDERDP (double precision version)
Authors/Contact	: Prof. Edward T. Pitkin
Program Funded by	: N. Conn., Research Foundation

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: N/A
Program Language	: Fortran IV
Computer Now Used	: IBM 360/65
Trajectory Options	: N/A
Input (briefly)	: Position and velocity at EPOCH
Parameters Optimized	: N/A
Other Applications	: Computes transition matrix, inverse 2nd partials, perturbative derivatives, etc.
Availability	: Single precision is share deck 3513; double precision version available from author.
Other comments	: Program is a general solution of two-body motion for all orbit shapes with 1st and 2nd partial derivatives plus perturbative derivatives for use in a variation of parameters integration.

Company/Organization	: General Dynamics/Convair
Name of Program	: Convair Low-Thrust Optimization Programs
Authors/Contact	: D. H. Higdon, J. F. Ingber, J. R. Grace
Program Funded by	: Company
	<u>Description</u>
Number of Dimensions	: 2, 3
Number of Bodies	: 2, N
Coordinate System	: Cartesian
Integration Technique	: Variable step, or fixed step
Program Language	: Fortran IV
Computer Now Used	: CDC 6400
Trajectory Options	: Flyby, rendezvous, fixed time, free time
Specific Impulse	: Variable or constant
Power Options	: Constant
Other Options	: Complete optimization from launch to capture (excluding spirals)
Initial Guesses Required	: Lagrange multipliers
Parameters Optimized (only μ_W in traj. part)	: Isp, T/W_O , μ_W , V_∞ , power level, coast time, thrust angle, final payload weight
Optimization Technique	: Newton-Raphson, maximum principle
Output (briefly)	: Time history, Isp, T/W, payload
Planetocentric Phase	: High-thrust capture and departure, low-thrust spiralling being developed
Documentation	: Limited
Availability	: Proprietary

Company/Organization	: General Dynamics/Fort Worth Division
Name of Program	: Y28 Optimum Low-Thrust Procedure
Authors/Contact	: JPL/M. Poteet (Fort Worth Div.)
Program Funded by	: Company

Description

Number of Dimensions	: 2, 3
Number of Bodies	: 2
Coordinate System	: Polar
Integration Technique	: Variable step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Variable, constant
Power Options	: Constant, function of time
Input (briefly)	: Position and velocity
Parameters Optimized	: $\int a^2 dt$
Optimization Technique	: Newton-Raphson
Output (briefly)	: $\int a^2 dt$
Planetocentric Phase	: Not included in program
Documentation	: JPL Engineer Planning Document #179
Availability	: Available from JPL
Other Comments	: JPL program is on production status at Fort Worth Division.

Company/Organization	: General Dynamics/Fort Worth Division
Name of Program	: Low-Thrust Trajectory Optimization
Authors/Contact	: D. H. Kruse
Program Funded by	: Company

Description

Number of Dimensions	: 2, 3
Number of Bodies	: 2
Coordinate System	: Cartesian, polar
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 36-
Trajectory Options	: Rendezvous
Specific Impulse	: Constant
Power Options	: Constant
Input (briefly)	: Julian dates, I_{sp} , α
Initial Guesses Required	: Lagrange multipliers, flight time
Parameters Optimized	: $\int a^2 dt$, coast time, thrust angle
Optimization Technique	: Newton-Raphson
Output (briefly)	: $\int a^2 dt$
Planetocentric Phase	: Not included in program
Other Comments	: Development of program is in initial phase.

Company/Organization	:	General Dynamics/Fort Worth Division
Name of Program	:	Interplanetary Low-Acceleration Constant- Thrust Trajectory Patching Program
Authors/Contact	:	S. W. Wilson/M. C. Poteet
Program Funded by	:	Company
		<u>Description</u>
Number of Dimensions	:	2
Number of Bodies	:	2
Integration Technique	:	None
Program Language	:	Fortran IV
Computer Now Used	:	IBM 7090
Trajectory Options	:	Planetocentric
Specific Impulse	:	Constant
Power Options	:	Constant
Input (briefly)	:	Position, effective exhaust velocity, K_{planet} , initial acceleration
Initial Guesses Required	:	Initial (final) acceleration in heliocentric orbit
Parameters Optimized	:	None
Output (briefly)	:	$\int a^2 dt$, "effective time to escape" (or capture), ΔV , mass ratio
Planetocentric Phase	:	Low-thrust spiralling
Limitations of Program	:	10^{-5} to 10^{-2} local "g" acceleration
Documentation	:	Customer Utilization Instructions, Procedure V06 (Co. document)
Availability	:	Proprietary, available under Government contract

Company/Organization : General Electric Co. - Advanced Nuclear
Systems Operation MSD

Name of Program : POLAR

Authors/Contact : Harold Brown

Program Funded by : Company

Description

Numbers of Dimensions : 2

Number of Bodies : 2

Coordinate System : Polar

Integration Technique : No integration used

Program Language : Fortran IV

Computer Now Used : IBM 7094

Trajectory Options : Flyby, rendezvous

Specific Impulse : Variable, constant

Power Options : Constant, function of time, function of
distance

Other Options : See comment.

Input (briefly) : Position and velocity, I_{sp} , α , V_{∞}

Parameters Optimized : T/W_0 , power level, coast time, thrust angle

Optimization Technique : Gradient method

Output (briefly) : Time history, payload, T/W

Planetocentric Phase : Not included in program

Limitations of Program : See comment.

Documentation : Incomplete

Availability : Not recommended at this time

Other Comments : Program attempts to find a trajectory which will
result in the specified power profile -
constant or variable. Results to date have
been unable to reduce deviations between the
actual and specified power profiles to less
than 10-15%.

Company/Organization	: General Electric - Missile and Space Division
Name of Program	: Finite Burn Orbit Insertion Program
Authors/Contact	: D. Korenstein
Program Funded by	: Company, NASA Contract

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, orbit insertion, escape
Specific Impulse	: Constant
Other Options	: 2-point boundary value problem for orbit insertion
Input (briefly)	: Hyperbola, ellipse, engine, guidance, planet
Parameters Optimized	: T/W_0
Optimization Technique	: Newton-Raphson
Output (briefly)	: Gravity loss
Planetocentric Phase	: High-thrust capture and departure, low-thrust spiralling
Other Applications	: Open-loop low-thrust trajectories
Documentation	: Not available
Availability	: Yes
Other Comments	: Program is partially checked out (in process)

Company/Organization	: NASA Goddard Space Flight Center
Name of Program	: Variable Power, Variable Thrust Option/F369
Contact	: Kenneth I. Duck, Aux. Prop. Br.
Program Funded by	: NAS 2-2928

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Variable
Power Options	: Constant, function of distance, function of time
Input (briefly)	: Julian dates, hyperbolic excess velocity, powerplant specific mass, initial power
Parameters Optimized	: $\int a^2 dt$
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history, $\int a^2 dt$
Planetocentric Phase	: Not included in program

Company/Organization : Goddard Space Flight Center, Mission and
Trajectory Analysis Division

Name of Program : Low-Thrust Trajectory Sub-Program

Contact : Robert T. Groves

Program Funded by : NASA Contract NAS 5-10029

Description

Number of Dimensions : 2 or 3

Number of Bodies : 2

Coordinate System : Cartesian

Integration Technique : Fixed step

Program Language : Fortran IV

Computer Now Used : IBM 7094

Trajectory Options : Rendezvous

Specific Impulse : Variable

Power Options : Constant

Input (briefly) : Position and velocity, hyperbolic excess
velocity

Initial Guesses Required : Program uses ballistic trajectory for first
fit

Parameters Optimized : $\int a^2 dt$, thrust angle

Optimization Technique : Newton-Raphson

Output (briefly) : Time history of thrust acceleration and
position, $\int a^2 dt$

Documentation : In progress

Availability : Program still under development

Company/Organization	: Grumman Aircraft, Bethpage, New York
Name of Program	: Low-Thrust Interplanetary Trajectory Optimization
Authors/Contact	: Hans K. Hinz and H. Gardner Moyer
Program Funded by	: NASA-MSFC, Contract No. NAS 8-1549

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 360/75
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Other Options	: Thrust constant, thrust variable but limited
Input (briefly)	: Position and velocity and orbital elements of target planet
Initial Guesses Required	: Control function(s)
Parameters Optimized	: Thrust angles and thrust magnitude
Optimization Technique	: Gradient method
Output (briefly)	: Time history
Planetocentric Phase	: Not included in program
Other Applications	: See Grumman report, RE-208, April 1965
Documentation	: See final report of Contract NAS 8-1549
Availability	: Nonproprietary availability to interested users
Other Comments	: RE-208 discusses GEOCENTRIC MISSIONS AND USE OF MORE EFFICIENT GENERALIZED NEWTON-RAPHSON METHOD OF OPTIMIZATION.

Company/Organization	: Hayes International Corp.
Name of Program	: Orbital Elements for Low Thrust Trajectories
Authors/Contact	: Harry Passmore
Program Funded by	: NASA Contract

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Orbital element
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: 1620 in part
Trajectory Options	: Near Earth spiral
Specific Impulse	: Constant
Other Options	: Constant thrust
Input (briefly)	: Position and velocity
Initial Guesses Required	: Lagrange multipliers
Parameters Optimized	: Thrust angle
Optimization Technique	: Calculus of variations
Output (briefly)	: Time history
Planetocentric Phase	: Low-thrust spiralling
Documentation	: NASA Report MTP-AERO-63-12
Other Comments	: Not presently operable

Company/Organization	: Hayes International Corp.
Name of Program	: Quasi-Steady Orbital Rendezvous
Authors/Contact	: Harry Passmore
Program Funded by	: NASA Contract

Description

Number of Dimensions	: 2
Number of Bodies	: Gravity of central body only
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 360
Trajectory Options	: Transfer
Specific Impulse	: Constant
Other Options	: Thrust magnitude constant
Input (briefly)	: Position and velocity, target position & velocity
Initial Guesses Required	: None
Parameters Optimized	: Thrust angle
Optimization Technique	: Maximum principle
Output (briefly)	: Time history
Planetocentric Phase	: Not included in program
Limitations of Program	: Initial longitude between vehicle & target $<90^\circ$
Documentation	: Hayes Engineering Report 1324
Availability	: Computer program not published
Other Comments	: Only used to date for circular orbit rendezvous

Company/Organization	: Hughes Aircraft Company
Name of Program	: Low-Thrust Trajectory
Authors/Contact	: D. MacPherson or J. H. Molitor
Program Funded by	: Partially Supported Under JPL Contract No. 951144

Description

Number of Dimensions	: 3
Number of Bodies	: N
Coordinate System	: Output in radius, ecliptic longitude, and normal to ecliptic
Integration Technique	: Variable step or fixed step
Program Language	: Fortran IV
Computer Now Used	: GE 635
Trajectory Options	: Flyby; rendezvous; round trip can be simulated by inputting cases sequentially.
Specific Impulse	: Constant
Power Options	: Function of time and/or function of distance
Other Options	: Program converges automatically to a trajec- tory which satisfies terminal conditions; optimization is by parameter search.
Input (briefly)	: Isp, powerplant specific mass, thrust profile, spacecraft mass, power profile, V_{∞} , launch date
Parameters Optimized	: Program converges automatically to a trajec- tory which satisfies terminal conditions.
Optimization Technique	: Parameter search
Output (briefly)	: Time history
Planetocentric Phase	: High-thrust capture, and departure
Documentation	: Not complete
Availability	: Subject to negotiation

Company/Organization	: IBM Federal Systems Division
Name of Program	: OPGUIDE
Authors/Contact	: G. W. Johnson, 1730 Cambridge Street Cambridge, Mass.
Program Funded by	: NASA Contract

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Variable step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094 - IBM System 360
Trajectory Options	: Rendezvous
Specific Impulse	: Variable
Power Options	: Function of time
Input (briefly)	: Position and velocity, Isp
Initial Guesses Required	: Lagrange multipliers
Parameters Optimized	: Coast time, thrust angle
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history
Other Applications	: High thrust orbital transfers
Documentation	: Preliminary
Availability	: Limited

Company/Organization	: IIT Research Institute
Name of Program	: LTNAV-1 (Low-Thrust Navigation Analysis)
Authors/Contact	: Alan L. Friedlander
Program Funded by	: NASA Contract 2-22401 and 2-3348

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian, polar
Integration Technique	: Variable step, fixed step
Program Language	: Fortran II
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Variable, constant
Power Options	: Constant
Input (briefly)	: Position and velocity
Initial Guesses Required	: Lagrange multipliers for converged optimal trajectory
Parameters Optimized	: Thrust angle
Optimization Technique	: Calculus of variations
Output (briefly)	: Time history
Other Applications	: Navigation studies
Documentation	: NASA CR-457

Company/Organization	: IIT Research Institute
Name of Program	: LTNAV-2 (Low-Thrust Planetocentric Navigation Analysis)
Authors/Contact	: ALAN L. Friedlander
Program Funded by	: NASA Contract 2-2401 and 2-3348

Description

Number of Dimensions	: 3
Number of Bodies	: 3
Coordinate System	: Cartesian
Integration Technique	: Variable step, fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Planetocentric only
Specific Impulse	: Constant
Power Options	: Constant
Other Options	: Constant acceleration
Input (briefly)	: Position and velocity, orbit elements
Output (briefly)	: Time history
Planetocentric Phase	: Program treats planetocentric phase only
Limitations of Program	: Tangential thrust only
Documentation	: NASA CR 740
Availability	: Yes, but documentation is negligible.

Company/Organization : JPL
Name of Program : Optimum Thrust Programs for Power Limited
Propulsion Systems (1016000)
Authors/Contact : Carl Sauer
Program Funded by : NASA Contract

Description

Number of Dimensions	: 2, 3
Number of Bodies	: 2
Coordinate System	: Polar
Integration Technique	: Variable step, fixed step
Program Language	: FAP
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous, solar probe, out of ecliptic, maximum energy
Specific Impulse	: Variable, constant
Power Options	: Constant, function of distance
Input (briefly)	: Position and velocity, Julian dates, hyperbolic excess velocity, Isp, power-plant specific mass, α
Initial Guesses Required	: Lagrange multipliers, T/W
Parameters Optimized	: Isp, T/W ₀ , μ_W , V_∞ , power level, $\int a^2 dt$, coast time, thrust angle
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history, Isp, T/W, payload, $\int a^2 dt$
Planetocentric Phase	: High-thrust capture and departure, low-thrust spiralling; approximations made to heliocentric portion using "asymptotic velocity bias." Spirals and high thrust escape can be run separately.
Other Applications	: Vehicle path optimization in vacuum
Documentation	: JPL EPD 179 11/1/63, latest documentation lacking
Availability	: Earlier version being used

Company/Organization	: JPL
Name of Program	: ASTRAL
Authors/Contact	: D. Alderson/W. Stavro
Program Funded by	: NASA Contract

Description

Number of Dimensions	: 3 (limited 3rd dimension)
Number of Bodies	: 2
Coordinate System	: Spherical
Integration Technique	: Analytic approximation
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Function of distance
Input (briefly)	: Julian dates, Isp, powerplant specific mass, planet (target, launch), powerplant efficiency
Parameters Optimized	: Isp, T/W_0 , μ_W , V_∞ , coast time, thrust angle
Optimization Technique	: "Complex" method
Output (briefly)	: Time history, Isp, T/W, payload
Planetocentric Phase	: High-thrust capture and departure
Limitations of Program	: Travel angle, T/local g, eccentricity of orbit
Initial Guesses Required	: None
Availability	: Not at present

Company/Organization	: JPL
Name of Program	: MALTS
Authors/Contact	: TRW Systems/J. Driver
Program Funded by	: NASA Contract NAS 7-503

Description

Number of Dimensions	: 3
Number of Bodies	: Up to 10
Coordinate System	: Spherical
Integration Technique	: Cowell or Adams Moulton
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Function of distance
Input (briefly)	: Position and velocity, Julian dates, excess velocity, Isp, powerplant specific mass, thrustor efficiency, time of flight
Initial Guesses Required	: Lagrange multipliers, or orbit plane
Parameters Optimized	: $\int a^2 dt$, time, final mass, payload
Optimization Technique	: Calculus of variations
Output (briefly)	: Time history, $\int a^2 dt$
Documentation	: User's Manual available

Description

Description

Description

Company/Organization : NASA Langley Research Center
 Name of Program : TOMSD (Trajectory Optimization by Method of
 Steepest Descent)
 Authors/Contact : Robert E. Smith
 Program Funded by : Air Force-NASA contract

Description

Number of Dimensions : 3
 Number of Bodies : 1 or more
 Coordinate System : Rectangular
 Integration Technique : Variable or fixed step
 Program Language : Fortran IV
 Computer Now Used : CDC 6000
 Trajectory Options : Reentry, boost, rendezvous
 Input (briefly) : Position and velocity
 Initial Guesses Required : Control history
 Parameters Optimized : Angle of attack, bank angle, initial state
 Optimization Technique : Gradient method
 Output (briefly) : Time history
 Planetocentric Phase : Not included in program
 Documentation : Technical Report AFFDL-TR-67-108, Vols. I, II, III
 Availability : Upon request
 Other Comments : This program is applicable to a variety of
 trajectory optimization problems.

Company/Organization	: NASA Lewis Research Center
Name of Program	: Lewis N-Body Code
Authors/Contact	: William C. Strack
Program Funded by	: Company

Description

Number of Dimensions	: 2, 3
Number of Bodies	: 2, 3, 8
Coordinate System	: Cartesian, orbit elements
Integration Technique	: Variable step, fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094, CDC 6600, IBM 7044
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Constant, function of distance
Other Options	: Targeting iteration, choice of thrust control
Input (briefly)	: Position and velocity, Julian dates, Isp, α , V_∞ , tank and structure fraction
Initial Guesses Required	: Lagrange multipliers, T/W, thrust angle α , $\dot{\alpha}$, etc.
Parameters Optimized	: Isp, T/W ₀ , V_∞ , power level, coast time, thrust angle
Optimization Technique	: Calculus of variations, univariate search
Output (briefly)	: Time history, payload
Planetocentric Phase	: High-thrust capture and departure, low-thrust spiralling
Other Applications	: Booster ascent paths
Documentation	: TN D-1730 with supplementary material
Availability	: Yes: 25 copies already sent out.
Other Comments	: Several versions of code exist (see NASA TM X52322).

LOW-THRUST TRAJECTORY AND MASS COMPUTATION PROGRAM

Company Organization : NASA-Lewis Research Center
 Name of Program : MAXIM
 Authors/Contact : E. A. Willis, Jr.
 Program Funded by : Lewis Research Center (in-house)

Description

Number of Dimensions : 2
 Number of Bodies : 2
 Coordinate System : Polar
 Integration Technique : Runge-Kutta with variable step size and error control
 Program Language : Fortran IV
 Computer Now Used : IBM 7094
 Trajectory Options : Orbit escape, capture, or transfer
 Specific Impulse : Constant I_{sp}
 Power Options : Constant power implied
 Other Options : Constant thrust, constant acceleration
 Input : Position and velocity; vehicle design parameters for each stage (up to 5)
 Initial Guesses Required : Initial positions and one multiplier (λ_0)
 Parameters Optimized : Thrust steering and switching program, staging points and acceleration levels are optimized for minimum ΔV or weight
 Optimization Technique : Maximum principle with conjugate-gradient search for the 2-point b.v.p.'s
 Output : Time history, ΔV 's, weights
 Documentation of Program : Theory and typical application covered in TN D-3606, TN D-4534, and TN D-5011.
 Availability to Other Users : Considered individually. Operating instructions are in the form of internal notes only.

Company/Organization : Research Laboratories; Lockheed Missiles
and Space Company

Name of Program : Low-Thrust Heliocentric Transfers

Authors/Contact : H. E. Rauch

Program Funded by : Company

Description

Number of Dimensions : 2 or 3

Number of Bodies : Vehicle plus up to three planets

Coordinate System : Cartesian

Integration Technique : Fixed step

Program Language : Fortran IV

Computer Now Used : Univac 1108

Trajectory Options : Flyby, rendezvous, and round trip with
variable acceleration only, rendezvous with
constant acceleration

Specific Impulse : Variable, constant

Power Options : Constant

Input (briefly) : Position and velocity of planets, elapsed
time

Initial Guesses Required : Lagrange multipliers

Parameters Optimized : $\int a^2 dt$, coast time, thrust angle for constant
acceleration

Optimization Technique : Guessing adjoint variables

Output (briefly) : Time history, $\int a^2 dt$

Planetocentric Phase : Not included in program

Limitations of Program : Not "production" type program

Documentation : "Low Thrust Swingby Trajectories," by
H. E. Rauch, XVIIIth International Astro-
nautical Congress - Belgrade, 1967, Pergamon
Press, Oxford, New York, PWN-Polish Scientific
Publishers, 1968, pp. 269-284.

Availability : Could be made available

Company/Organization : Research Laboratories, Lockheed Missiles
and Space Co.

Name of Program : Low-Thrust Escape From Planet

Authors/Contact : H. E. Rauch

Program Funded by : Company

Description

Number of Dimensions : 2

Number of Bodies : 2

Coordinate System : Both, but primarily polar

Integration Technique : Variable step

Program Language : Fortran IV

Computer Now Used : Univac 1108

Specific Impulse : Variable, constant acceleration

Power Options : None, trajectory with constant acceleration
in velocity direction

Input (briefly) : Initial position and velocity, final desired
hyperbolic excess velocity, constant or
"average" acceleration

Initial Guesses Required : Lagrange multipliers

Parameters Optimized : $\int a^2 dt$, thrust angle for constant acceleration

Optimization Technique : Guessing adjoint variables

Output (briefly) : Time history, $\int a^2 dt$

Planetocentric Phase : Low-Thrust spiralling

Limitations of Program : Not "production" type program

Other Applications : Uses asymptotic matching to calculate
heliocentric "offsets"

Documentation : "Optimum Guidance for a Low Thrust Interplane-
tary Vehicle," J. Breakwell and H. Rauch,
AIAA Journal, Vol. 4, No. 4, April 1966

Availability : Could be made available

Company/Organization : Lockheed Missiles & Space Co./Advanced
Flight Mechanics

Name of Program : LTCØMP

Authors/Contact : M. A. Krop, Dept. 55-34, B. 201, Ext. 45869

Program Funded by : Company

Description

Number of Dimensions : 2, 3

Number of Bodies : 4

Coordinate System : Planet-center & aligned along the excess
velocity vectors

Integration Technique : None

Program Language : Fortran IV

Computer Now Used : Univac 1108

Trajectory Options : Single-leg interplanetary transfer

Specific Impulse : Variable, constant

Power Options : Constant

Input (briefly) : Julian dates, planet numbers

Initial Guesses Required : Time offsets at terminal planets

Parameters Optimized : $\int a^2 dt$

Optimization Technique : Analytic approximation

Output (briefly) : $\int a^2 dt$

Planetocentric Phase : Not included in program

Limitations of Program : Travel angle

Documentation : Method described in Chapter 4 of LMSC
Rept. No. 3-17-64-1, Apr. 30, 1964

Availability : Still being developed

Other Comments : LTCØMP rapidly simulates the propulsion
requirements for a low-thrust transfer.
Although quite simplified, it computes
optimum $\int a^2 dt$ to within a couple of
percent of rigorously optimized values.

Company/Organization : Los Alamos Scientific Laboratory, Los Alamos,
New Mexico

Name of Program : 1965 Version, produced by Dept. of Aerospace
and Mechanical Sciences, Princeton Univ.,
Report No. 7170-1

Program Funded by : AEC

Description

Number of Dimensions : 2

Number of Bodies : 2

Coordinate System : Polar

Integration Technique : Variable step

Program Language : Fortran IV

Computer Now Used : IBM 7094, IBM 7030

Trajectory Options : Rendezvous

Specific Impulse : Constant

Power Options : Constant (with coast)

Input (briefly) : Position and velocity, Isp

Initial Guesses Required : Lagrange multipliers

Parameters Optimized : Coast time, thrust angle

Optimization Technique : Direct

Output (briefly) : Time history, T/W

Planetocentric Phase : Not included in program

Company/Organization	: McDonnell Douglas Astronautics Company
Name of Program	: FYNDIF
Authors/Contact	: F. I. Mann
Program Funded by	: Company

Description

Number of Dimensions	: 2
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Second order finite difference procedure
Program Language	: Fortran IV
Computer Now Used	: Univac 1108
Trajectory Options	: Rendezvous, intercept
Input (briefly)	: Position and velocity, hyperbolic excess velocity
Parameters Optimized	: $\int a^2 dt$
Optimization Technique	: Calculus of variations and Van Dine's Generalized Newton-Raphson
Output (briefly)	: Time history
Planetocentric Phase	: Not included in program
Limitations of Program	: Experimental program, planets in circular orbits, few options

Company/Organization	: McDonnell Douglas Astronautics Company
Name of Program	: LOWTOP, High-Low Thrust Trajectory Optimization Program
Authors/Contact	: Jerry L. Horsewood/F. I. Mann
Program Funded by	: Company

Description

Number of Dimensions	: 2
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Variable step, fourth-order Runge Kutta
Program Language	: Fortran IV
Computer Now Used	: Univac 1108
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Variable, constant
Power Options	: Constant or variable
Input (briefly)	: Position and velocity, Julian dates, V_{∞} , Isp, thrust, power, weight-flow
Initial Guesses Required	: Lagrange multipliers
Parameters Optimized	: $\int a^2 dt$, coast time, thrust angle, flight time, final speed
Optimization Technique	: Newton-Raphson, maximum principle
Output (briefly)	: Time history, Isp, T/W, velocity loss
Planetocentric Phase	: High-thrust capture and departure
Other Applications	: See company documentation on LOWTOP
Documentation	: First draft complete
Availability	: Currently not available

Company/Organization	: McDonnell Douglas Astronautics Company
Name of Program	: WHAMO, Weight History and Mission Optimizer
Authors/Contact	: F. I. Mann
Program funded by	: Company

Description

Number of Dimensions	: 2
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Variable step, Fourth-order Runge Kutta
Program Language	: Fortran IV
Computer Now Used	: Univac 1108
Trajectory Options	: Rendezvous, round trip, multi-leg missions
Specific Impulse	: Variable or constant
Power Options	: Variable or constant
Input (briefly)	: Julian dates, hyperbolic excess velocity, Isp, thrust, power, weight flow
Initial Guesses Required	: Lagrange multipliers, T/W
Parameters Optimized	: Isp, coast time, thrust angle, gross weight
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history, Isp, T/W
Planetocentric Phase	: High capture and departure with engine shutdown & restart
Other Applications	: Simulates both high and low thrust engine shutdown and restart with high thrust staging according to the non-integral-burn method
Documentation	: Partial
Availability	: Currently not available
Other Comments	: Program not extensively used yet

Company/Organization : McDonnell Douglas Astronautics Company
Name of Program : HITOP
Authors/Contact : F. I. Mann
Program Funded by : Company

Description

Number of Dimensions	:	3
Number of Bodies	:	2
Coordinate System	:	Cartesian
Integration Technique	:	Impulse trajectories analytic solution
Program Language	:	Fortran IV
Computer Now Used	:	Univac 1108
Trajectory Options	:	Rendezvous
Input (briefly)	:	Julian dates
Initial Guesses Required:	:	Time and place of deep space impulse
Parameters Optimized	:	Either $(V_{\infty 1} + \Delta V_2 + V_{\infty 3})$ or $(\Delta V_1 + \Delta V_2 + \Delta V_3)$
Optimization Technique	:	Newton-Raphson or transversality procedure
Output (briefly)	:	Primer vector, V_{∞} , ΔV , orbit parameters
Planetocentric Phase	:	High-thrust capture and departure
Limitations of Program	:	Currently only one deep-space impulse
Other Applications	:	Program may be used to study the high-thrust limit of low-thrust trajectories.
Documentation	:	None
Availability	:	Currently not available

Company/Organization	: Space Division, North American Rockwell Corp.
Name of Program	: Optimum Trajectory Program for Power-Limited Propulsion Systems
Authors/Contact	: Russell P. Nagorski
Program Funded by	: Company

Description

Number of Dimensions	: 3
Number of Bodies	: 4
Coordinate System	: Polar
Integration Technique	: Fixed step
Program Language:	: I II
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Variable, constant
Power Options	: Constant
Input (briefly)	: Position and velocity, Julian dates, V_{∞} , Isp, α
Initial Guesses Required	: Lagrange multipliers, T/W
Parameters Optimized	: $\int a^2 dt$, coast time
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history, Isp, T/W, payload, $\int a^2 dt$
Planetocentric Phase	: Not included in program
Limitations of Program	: Initial guess, iteration logic
Other Applications	: General intercept and rendezvous problems
Documentation	: User's Manual complete
Other Comments	: Derivative of JPL (Melbourne and Sauer) program

Company/Organization	: Mission Analysis Division, OART/NASA
Name of Program	: BABE
Authors/Contact	: A. C. Mascy/S. W. Pitts
Program Funded by	: In-house

Description

Number of Dimensions	: 2
Number of Bodies	: 2
Coordinate System	: Polar
Integration Technique	: Variable step and fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Constant
Input (briefly)	: Julian dates, hyperbolic excess velocity, α
Parameters Optimized	: Isp, μ_W , coast time
Optimization Technique	: Gradient method
Output (briefly)	: Coast time, Isp, payload, μ_W
Planetocentric Phase	: High-thrust capture and departure, low-thrust spiralling
Documentation	: In progress

Company/Organization : Mission Analysis Division, OART/NASA
 Name of Program : QUICKLY
 Authors/Contact : Alfred C. Masey
 Program Funded by : In-house

Description

Number of Dimensions	{	Program uses functional relationships for the energy requirements of pre-computed built-in performance data which were obtained by accurate 3-dimensional, 2-body, Cartesian coordinate, Newton-Raphson finite-difference programs.
Number of Bodies		
Coordinate System		
Integration Technique		
Program Language	:	Fortran IV
Computer Now Used	:	IBM 360/50
Trajectory Options	:	Flyby, rendezvous, solar probe, extra-ecliptic, comet intercept
Specific Impulse	:	Constant
Power Options	:	Constant, function of time or distance
Other Options	:	Optimum or fixed power level or alpha as a function of power. Also, optimum or fixed hyperbolic excess velocities
Input (briefly)	:	Trip time, power plant specific mass α , launch vehicle name, capture and departure mode
Initial Guesses Required	:	None
Parameters Optimized	:	Isp, μ_W , $V_{\infty 1}$, $V_{\infty 2}$, power level, coast time
Optimization Technique	:	Gradient method and Newton-Raphson
Output (briefly)	:	Payload, Isp, μ_W , $V_{\infty 1}$, $V_{\infty 2}$, power level, powered time, also, plot option
Planetocentric Phase	:	High-thrust capture and departure, low-thrust spiralling, launch vehicle boost
Other Applications	:	May be used to determine performance of two-impulse ballistic systems for comparisons
Documentation	:	In progress
Availability	:	Upon request

Company/Organization : ASMAR, Princeton University
Name of Program : Lion 1
Authors/Contact : J. Campbell/P. M. Lion
Program Funded by : NASA contract

Description

Number of Dimensions	:	3
Number of Bodies	:	2
Coordinate System	:	Cartesian
Integration Technique	:	Variable step
Program Language	:	Fortran IV
Computer Now Used	:	IBM 7094, CDC 6600, IBM 360/50
Trajectory Options	:	Flyby, rendezvous, round trip, escape*
Specific Impulse	:	Constant
Power Options	:	Constant, function of time, function of distance
Other Options	:	Booster selection
Input (briefly)	:	Position and velocity or Julian dates, power plant specific mass, tankage, structure factors
Initial Guesses Required	:	Lagrange multipliers
Parameters Optimized	:	Isp, T/W_O , μ_W , V_∞ , power level, coast time, thrust angle*
Optimization Technique	:	Neighboring extremal
Output (briefly)	:	Time history, Isp, T/W, payload
Planetocentric Phase	:	High-thrust capture and departure
Other Applications	:	Iterator can be used to solve <u>any</u> nonlinear (algebraic) equations.
Documentation	:	In progress
Availability	:	Available on request
Other Comments	:	*Other options available depending on input

Company/Organization	: ASMAR, Princeton University
Name of Program	: Campbell 1 (Modified Item)
Authors/Contact	: J. Campbell/P. M. Lion
Program Funded by	: NASA contract

Description

Number of Dimensions	: 3
Number of Bodies	: 9
Coordinate System	: Cartesian
Integration Technique	: Variable step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094, IBM 360/50
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Constant, function of time, function of distance
Other Options	: Programmed thrust
Input (briefly)	: Position and velocity or Julian dates
Initial Guesses Required	: Lagrange multipliers
Optimization Technique	: Neighboring extremal
Planetocentric Phase	: Included in program
Other Applications	: Uses generalized iterator
Documentation	: Partially complete
Availability	: Difficult to transfer
Other Comments	: Used mainly as check on 2-body program

Company/Organization : ASMAR, Princeton University
 Name of Program : Gordon 2
 Authors/Contact : C. N. Gordon/P. M. Lion
 Program Funded by : NASA contract

Description

Number of Dimensions : 2
 Number of Bodies : 2
 Coordinate System : Polar
 Integration Technique : Fixed step
 Program Language : Fortran IV
 Computer Now Used : IBM 7094, CDC 6600 (now being adapted),
 IBM 360/50
 Trajectory Options : Flyby, rendezvous, round trip, constrained
 velocity flyby
 Specific Impulse : Constant
 Power Options : Constant, function of time, function of
 distance
 Other Options : Select booster
 Input (briefly) : Position and velocity or Julian dates (can
 input or optimize: excess velocity, Isp),
 power plant specific mass, α , tankage,
 structure factors
 Initial Guesses Required : Lagrange multipliers
 Parameters Optimized : Isp, T/W_0 , μ_W , V_∞ , power level, direction
 of arrival velocity, coast time, thrust
 angle, C_3
 Optimization Technique : Neighboring extremal
 Output (briefly) : Time history, Isp, T/W , payload, summary
 Planetocentric Phase : High-thrust capture and departure
 Documentation : In progress
 Availability : Available on request
 Other Comments : Also being used at Battelle, IITRI, MSFC

Company/Organization	: ASMAR, Princeton University
Name of Program	: PRIMER
Authors/Contact	: M. Minkoff/P. M. Lion
Program Funded by	: NASA contract

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Impulsive trajectories analytic solution
Program Language	: Fortran IV
Computer Now Used	: IBM 7094
Trajectory Options	: Flyby, rendezvous
Input (briefly)	: Position and velocity or Julian dates
Optimization Technique	: Conjugate gradient
Output (briefly)	: Time history, $J = \sum_i \Delta \vec{V}_i $
Planetocentric Phase	: High-thrust capture and departure
Documentation	: In thesis form
Availability	: Available on request
Other Comments	: Finds optimum impulsive trajectory regardless of the number of impulses

Company/Organization : Rand Corp.
 Name of Program : ROCKET
 Authors/Contact : B. W. Boehm
 Program Funded by : USAF Project RAND

Description

Number of Dimensions : 3
 Number of Bodies : 4
 Coordinate System : Cartesian, polar
 Integration Technique : Variable step, fixed step, Cowell method
 Program Language : Fortran IV, II
 Computer Now Used : IBM 7094, CDC 6600, Univac 1108, GE 635
 Trajectory Options : Flyby, departure and capture
 Specific Impulse : Variable, constant
 Power Options : Constant, function of time
 Other Options : Numerous propulsion, aerodynamic, guidance
 options
 Input (briefly) : Position and velocity
 Output (briefly) : Time history, Isp, T/W, osculating orbit
 parameters, tracking obs.
 Planetocentric Phase : High-thrust capture and departure, low-thrust
 spiralling
 Limitations of Program : Cowell method makes ROCKET inefficient for
 long-duration trajectories.
 Other Applications : Boost, reentry, airbreathing propulsion
 Documentation : Book: ROCKET, by B. W. Boehm, Prentice-Hall,
 1964
 Availability : Through SHARE Distribution Agency, 112 E. Post
 Road, White Plains, New York (send blank mag.
 tape, ask for #3001 (Fortran II version)
 or #3485 (Fortran IV version))

Company/Organization	: RCA/Astro Electronics Division
Name of Program	: Gordon 2
Authors/Contact	: C. N. Gordon/J. M. L. Holman
Program Funded by	: Company, NASA contract

Description

Number of Dimensions	: 2
Number of Bodies	: 2
Coordinate System	: Polar
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: IBM 7094, IBM 360/50
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Constant, function of time, function of distance
Other Options	: Choice of launch vehicle, sweep of parameters
Input (briefly)	: Julian dates, power plant specific mass
Initial Guesses Required	: Lagrange multipliers, T/W, power, C_3
Parameters Optimized	: Isp, T/W_0 , V_∞ , power level, coast time, thrust angle, C_3
Optimization Technique	: Neighboring extremal
Output (briefly)	: Time history, Isp, T/W, payload
Planetocentric Phase	: High-thrust capture and departure
Documentation	: In progress
Availability	: Available through ASMAR, Princeton University

Company/Organization : System Sciences Corp. (Subsidiary of Computer Science Corp.)

Name of Program : High-Precision, Low-Thrust Integration and Optimization Prog.

Authors/Contact : Pitkin and Baker/Dr. R. M. L. Baker, Jr.

Program Funded by : Company

Description

Number of Dimensions : 3

Number of Bodies : Any number for which ephemerides are given

Coordinate System : Cartesian

Integration Technique : Variable step

Program Language : II

Computer Now Used : IBM 7094

Trajectory Options : Open

Specific Impulse : Variable

Power Options : Function of time

Input (briefly) : Position and velocity, Isp

Initial Guesses Required : Lagrange multipliers

Parameters Optimized : Power level

Optimization Technique : Gradient method

Output (briefly) : Time history

Planetocentric Phase : Low-thrust spiralling

Other Applications : Can interface with other impulsive thrust programs

Documentation : Listing of basic program

Availability : Yes

Other Comments : Utilizes universal variable so that it can pass evenly from ellipses through parabolas, to hyperbolas

Company/Organization : U. of Texas, Austin, Dept. of Aerospace Eng.
 Name of Program : NMS
 Authors/Contact : G. J. Lastman & W. T. Fowler
 Program Funded by : NASA contract and graduate student and faculty
 time contributions

Description

Number of Dimensions : 3
 Number of Bodies : 2
 Coordinate System : Cartesian
 Integration Technique : Fixed step
 Program Language : Fortran IV
 Computer Now Used : CDC 6600
 Trajectory Options : Rendezvous
 Specific Impulse : Constant
 Power Options : Constant
 Input (briefly) : Position and velocity, or Julian dates
 Initial Guesses Required : Lagrange multipliers
 Parameters Optimized : $\int a^2 dt$, flight time
 Optimization Technique : Perturbation
 Output (briefly) : Time history, initial multipliers
 Planetocentric Phase : Not included in program, capture being
 implemented
 Limitations of Program : Travel time limit of ≈ 1000 days
 Documentation : Limited
 Availability : Listing and/or deck on request

Company/Organization : TRW Systems/Analytic Mechanics Dept.
 Name of Program : MALTS, Mission Analysis & Simulation Program
 Authors/Contact : D. B. Smith & W. D. Dickerson (R3/T, 3442)
 Program Funded by : NASA contract

Description

Number of Dimensions : 3
 Number of Bodies : N
 Coordinate System : Cartesian
 Integration Technique : Variable step, fixed step (both)
 Program Language : Fortran IV
 Computer Now Used : IBM 7094
 Trajectory Options : Flyby, rendezvous
 Specific Impulse : Variable, constant
 Power Options : Constant, function of time, function of distance
 Other Options : Nonoptimal or optimal steering, computed or tabular thrust, others, see report
 Input (briefly) : Position and velocity or Julian dates, V_{∞} , Isp, α
 Initial Guesses Required : Steering angles
 Parameters Optimized : Can optimize any selected parameter
 Optimization Technique : Newton-Raphson (modified)
 Output (briefly) : Time history, Isp, T/W, payload
 Planetocentric Phase : High-thrust capture and departure
 Limitations of Program : Optimal phasing logic not included yet
 Documentation : User's Guide (Vol. I & II), Interim Report NAS 7-503
 Availability : See John Driver, JPL
 Other Comments : The program is not completely ready for general use.

Company/Organization : United Aircraft Research Laboratories
 Name of Program : Mass ratio optimization (simplified & improved
 payload fraction definition) F487
 Authors/Contact : R. Ragsac/Betty Knose
 Program Funded by : Company

Description

Number of Dimensions : 3
 Number of Bodies : 2
 Coordinate System : Cartesian
 Integration Technique : Fixed step
 Program Language : Fortran V
 Computer Now Used : Univac 1108
 Trajectory Options : Rendezvous
 Specific Impulse : Constant
 Power Options : Constant
 Input (briefly) : Julian dates, V_{∞} , α , η , thruster specific mass
 curve
 Initial Guesses Required : I_{sp} , μ_1
 Parameters Optimized : I_{sp} , μ_w , $\int a^2 dt$, coast time
 Optimization Technique : Newton-Raphson
 Output (briefly) : I_{sp} , $\int a^2 dt$, μ_w , μ_1 , μ_L powered time
 Planetocentric Phase : Not included in program
 Limitations of Program : Travel angle, powered time is approximate
 Documentation : Sample input and explanation
 Availability : Yes
 Other Comments : Differs from F530 in capability to maximize
 realistic definition for payload fraction

Company/Organization : United Aircraft Research Laboratories
 Name of Program : High & Low Thrust Mass Optimization/F211
 Authors/Contact : Betty Knose/R. Ragsac
 Program Funded by : NASA Contract NAS 2-2928

Description

Number of Dimensions : 2 or 3
 Number of Bodies : 2
 Coordinate System : See other comments
 Integration Technique : See other comments
 Program Language : Fortran V
 Computer Now Used : Univac 1108
 Trajectory Options : Flyby, rendezvous, round trip
 Specific Impulse : Constant
 Input (briefly) : α , high and low-thrust propulsion parameters,
 table of μ_L , μ_w Isp vs. V_∞
 Initial Guesses Required : None
 Parameters Optimized : Mass on Earth parking orbit
 Optimization Technique : Search
 Output (briefly) : System masses and propulsion parameters
 Planetocentric Phase : Hyperbolic excess speeds (high-thrust system)
 Documentation : User's Manual
 Availability : See NASA, MAD
 Other Comments : Mass optimization only; trajectory data
 are input

Company/Organization	: United Aircraft Research Laboratories
Name of Program	: Mass Ratio Optimization (simplified payload fraction) F530
Authors/Contact	: R. Ragsac/Betty Knose
Program Funded by	: Company

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran V
Computer Now Used	: Univac 1108
Trajectory Options	: Rendezvous
Specific Impulse	: Constant
Power Options	: Constant
Input (briefly)	: Julian dates, V_{∞} , α
Initial Guesses Required	: None
Parameters Optimized	: I_{sp} , μ_w , $\int a^2 dt$, coast time
Optimization Technique	: Newton-Raphson
Output (briefly)	: I_{sp} , $\int a^2 dt$, μ_w , μ_L , μ_1 powered time
Planetocentric Phase	: Not included in program
Limitations of Program	: Travel angle $\sim 3\pi$, powered time is approximate
Documentation	: Sample input and explanation
Availability	: Yes
Other Comments	: Optimization of I_{sp} and μ_w uses accurate approximation technique, single coast period only

Company/Organization	: United Aircraft Research Laboratories
Name of Program	: Variable Power, Variable Thrust Option/F369
Authors/Contact	: Mrs. E. Knose, Mr. G. Thrasher, UARL
Program Funded by	: NASA Contract NAS 8-11309, NAS 2-2928

Description

Number of Dimensions	: 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran IV
Computer Now Used	: Univac 1108, Fortran V
Trajectory Options	: Flyby, rendezvous, solar probe
Specific Impulse	: Variable
Power Options	: Constant, function of time, function of distance
Input (briefly)	: Position and velocity, Julian dates, V_{∞} , power option input
Initial Guesses Required	: None
Parameters Optimized	: $\int a^2 dt$
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history, $\int a^2 dt$
Planetocentric Phase	: Not included in program
Documentation	: Sample input and explanation
Availability	: Determined by NASA

Company/Organization	: United Aircraft Research Laboratories
Name of Program	: Constant-Thrust, Multiple-Coast/F615
Authors/Contact	: C. P. Van Dine/Betty Knose
Program Funded by	: NASA Contract NAS 2-2928

Description

Number of Dimensions	: 2 or 3
Number of Bodies	: 2
Coordinate System	: Cartesian
Integration Technique	: Fixed step
Program Language	: Fortran V
Computer Now Used	: Univac 1108
Trajectory Options	: Flyby, rendezvous
Specific Impulse	: Constant
Power Options	: Constant
Other Options	: Optimize Isp and μ_w , fix μ_w opt Isp, fix Isp opt μ_w , or input Isp and μ_w
Input (briefly)	: Julian dates, V_∞ , α , efficiency parameter
Initial Guesses Required	: None
Parameters Optimized	: Isp μ_w , $\int a^2 dt$, coast time
Optimization Technique	: Newton-Raphson
Output (briefly)	: Time history, Isp, payload, $\int a^2 dt$, powered times
Planetocentric Phase	: Not included in program
Limitations of Program	: Travel angle $\sim 3\pi$
Documentation	: Programmer's Manual, UARL F-910352-13
Availability	: See NASA, MAD
Other Comments	: Two heliocentric coast periods allowed

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